

Numerical tools for optimization

Subject Information	
Code	UE3 S3
Credits (ECTS)	7
Semester	2 (mid-January - June)
Time Allocation (Lec. / Prac. / Lab/ Project)	20 h / 30 h / 0 / 50 h
Lecturer	Pr. Jean-Michel RENAUME, Dr Sylvain SERRA.
Pre-requisites	
Assessment	Final written examination + project

Lec. : Lectures

Prac. : Practical works ("small classes")

Lab.: Laboratories

Subject Description	
Introduction	Optimization is one of the major quantitative tools for decision-making. Acquainting students with the optimization problem formulation (objective function, optimization variables and constraints) and solution (algorithms and software tools) is the primary aim of this subject.
Learning outcomes	<p>After this course, students should:</p> <ul style="list-style-type: none"> - be able to formulate an optimization problem - be able to characterize the formulated problem (LP, NLP, MILP, MINLP...) and select an appropriate optimization algorithm (Simplex, SQP, Branch and Bound, OA/ER) - have a basic knowledge of the main algorithm - be able to use the main tools: Excel®, GAMS®
Content	<p>I. Introduction Motivation, scope, general formulation procedure, examples...</p> <p>II. Unconstrained Optimization</p> <ol style="list-style-type: none"> 1. Basic Concepts Continuity, convexity, extremum, necessary and sufficient condition... 2. One-dimensional Search Scanning and bracketing procedure, Newton-like method... 3. Multivariable Optimization Direct methods, indirect methods, random search...

- III. Continuous Constrained Optimization**
 - 1. Linear Programming
Simplex method
 - 2. The Theory of Constrained Optimization
Lagrange multipliers, first and second order condition, duality...
 - 3. Quadratic Programming
Equality constraints, active set method...
 - 4. Non Linear Programming
Penalty function, Successive Quadratic Programming,
- IV. Discrete Constrained Optimization**
 - 1. Dynamic Programming
Bellman's principle
 - 2. Mixed-Integer Programming
Multi-period optimization, Branch and Bound
 - 3. Mixed-Integer Non Linear Programming
Bender's decomposition, Outer Approximation...
- V. Multi-objective Optimization**
Pareto optimal solution, ε -constraints Method, random search...
- VI. Dynamic Optimization**
 - 1. Multi-period optimization
 - 2. Discretization Methods
Control Vector Parametrization
 - 3. Variational Methods
Optimal control, Pontryagin's Maximum Principle...
- VII. Global Optimization**
Stochastic/deterministic methods
- VIII. Process Optimization**
 - 1. General Environments
GAMS, Excel...
 - 2. Flowsheeting Environments
ProSim Plus...

Typical Projects:

Heat Exchanger Network (HEN) Optimization
 Synthesis of General Distillation Sequences
 Pump Network Synthesis

Literature

Nonlinear and Mixed-Integer Optimization – Fundamentals and Applications. C.A. Floudas. Oxford University Press, 1995
Practical Methods of Optimization. R. Fletcher. Second Edition. Wiley-Interscience Publication, 1996
Optimization of Chemical Processes. T.F. Edgar and D.M. Himmelblau. McGraw-Hill International Editions, 1989.